

Calculus 1

Unit 5 Quiz 2 Review

Part I: No GRAPHING Calculators are permitted in this section!

1. Write out the terms for the given sequence and find the sum of each. (SHOW YOUR WORK!)

a) $\sum_{n=1}^6 (2n + 3)$

b) $\sum_{n=2}^5 (3n^2 + 1)$

2. Write the following sum using sigma notation.

a) $5+7+9+11+13+15+17$

b) $\frac{1}{3} + \frac{1}{9} + \frac{1}{27} + \dots + \frac{1}{2187}$

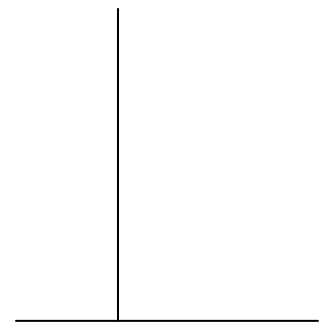
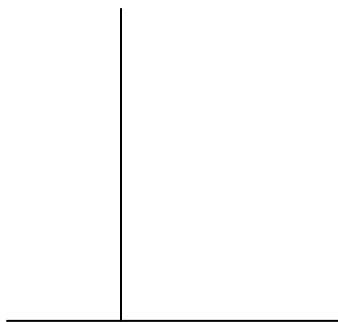
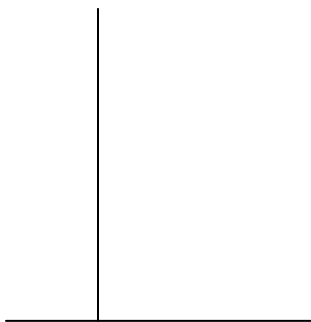
3. Use your special formulas to evaluate the following. (SHOW YOUR WORK!)

a) $\sum_{k=1}^{12} (2k^3 - 2k + 7)$

b) $\sum_{k=6}^{18} (3k^2 + 2k)$

4. Draw the graph for the function and use LRAM, RRAM, and MRAM to approximate the area under the curve in the given interval for n rectangles.

$f(x) = x^2 + 2$ $[-2,4]$ $n=6$



Part II: GRAPHING Calculators are permitted in this section!**5. Apply the definite integral properties to the following to solve.****GIVEN:**

$$\int_0^3 f(x)dx = 7, \int_3^7 f(x)dx = 17, \int_0^3 g(x)dx = 4$$

a) $\int_7^0 f(x)dx =$

b) $\int_0^3 [6g(x) - 3f(x)]dx =$

6. Use your calculator to find the following sums.

a) $\sum_{k=20}^{42} (3k^2 + 4k - 5)$

b) $\sum_{k=2}^{15} (-1)^k (k^2 - 4k)$

7. Use your calculator to approximate the area under the curve using the indicated method (LRAM, RRAM, and MRAM) over the given interval for n rectangles.

Use LRAM: $f(x) = x^3 + 2x + 7$ $[-5,5]$ $n=50$

Use RRAM: $f(x) = \sqrt{x} + 4$ $[0,6]$ $n=60$

Use MRAM: $f(x) = 5 + x + 2x^2$ $[0,4]$ $n=100$

8. Evaluate the definite integrals.

a) $\int_{-2}^4 (6x^2 - 10x + 3)dx$

b) $\int_{\frac{\pi}{2}}^{\pi} \cos x dx$

c) $\int_0^1 (4x+1)^5 dx$

d) $\int_0^3 \frac{t}{(t^2+3)^2} dt$

e) $\int_1^2 \frac{x^3 - 16}{x^2} dx$

SOLUTIONS

1. a) 60

b) 166

2. a) $\sum_{k=0}^6 2k + 5$

b) $\sum_{k=1}^7 \frac{1}{3^k}$

3. a) 12096

b) 6474

4. LRAM: $31 u^2$

RRAM: $43 u^2$

MRAM: $35.5 u^2$

5. a) -24

b) 3

6. a) 72,082

b) -91

7. LRAM: $43 u^2$

RRAM: $33.9 u^2$

MRAM: $70.67 u^2$

8. a) 102

b) -1

c) 651

d) .125 or $\frac{1}{8}$

e) -6.5

SOLUTIONS

1. a) 60

b) 166

2. a) $\sum_{k=0}^6 2k + 5$

b) $\sum_{k=1}^7 \frac{1}{3^k}$

3. a) 12096

b) 6474

4. LRAM: $31 u^2$

RRAM: $43 u^2$

MRAM: $35.5 u^2$

5. a) -24

b) 3

6. a) 72,082

b) -91

7. LRAM: $43 u^2$

RRAM: $33.9 u^2$

MRAM: $70.67 u^2$

8. a) 102

b) -1

c) 651

d) .125 or $\frac{1}{8}$

e) -6.5